

Why are batteries/pop cans cylinders?

- easy to hold
- easy to manufacture
- structural strength

For a fixed volume, the cylinder will reduce surface area.

Comparing prisms/cylinders:

$$V = A_b \cdot h$$

↑ fixed ↑ fixed ← must be the same

$$SA = 2A_b + A_s$$

$$= 2A_b + P_b \cdot h$$

↑ fixed ↑ same

minimizing perimeter, minimizes SA and circle is best

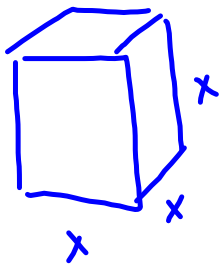
Given equivalent rectangular prisms, which dimensions will produce the smallest surface area?

CUBE!

Since square will minimize perimeter of base

A rectangular prism has a volume of 9261cm^3 , what is the minimum surface area?

cube



$$V = x^3$$

$$9261\text{cm}^3 = x^3$$

$$\sqrt[3]{9261\text{cm}^3} = x$$

$$x = 21\text{cm}$$

$$SA = 2A_b + A_e$$

$$= 2A_b + P_b h$$

$$= 6x^2 \leftarrow \text{for cube}$$

$$= 6(21\text{cm})^2$$

$$= 2646\text{cm}^2$$

Given any equivalent solids, which solid will produce the smallest surface area?

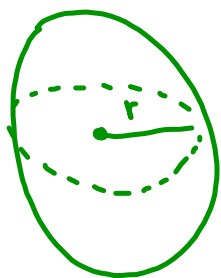
SPHERE

$$V = \frac{4}{3}\pi r^3$$

$$SA = 4\pi r^2$$

A solid has a surface area of 804 dm^2 . What is the maximum volume of the solid?

sphere



$$SA = 4\pi r^2$$

$$\frac{804 \text{ dm}^2}{4} = \frac{4\pi r^2}{4}$$

$$\frac{201 \text{ dm}^2}{\pi} = \frac{\pi r^2}{\pi}$$

$$63.98 \text{ dm}^2 = r^2$$

$$r = \sqrt{63.98 \text{ dm}^2}$$

$$r = 8 \text{ dm}$$

$$\begin{aligned} V &= \frac{4}{3}\pi r^3 \\ &= \frac{4}{3}\pi (8 \text{ dm})^3 \\ &= 2144.7 \text{ dm}^3 \end{aligned}$$

p.125 #1-4
online assignment