

While still on the top of the school (15 m high) a second egg is thrown straight upwards with an initial speed of 8.0 m/s.

a) What is the maximum height reached by the egg?

$$\vec{v}_i = 8.0 \text{ m/s [up]}$$

$$\vec{v}_f = 0 \text{ (stops at max height)}$$

$$\vec{a}_g = 9.8 \text{ m/s}^2 \text{ [down]}$$

$$\vec{\Delta d} = ?$$

always for free fall

$$\vec{v}_f^2 = \vec{v}_i^2 + 2\vec{a}\vec{\Delta d}$$

$$\frac{\vec{v}_f^2 - \vec{v}_i^2}{2\vec{a}} = \vec{\Delta d}$$

$$\frac{0^2 - (+8)^2}{2(-9.8)} = \vec{\Delta d}$$

$$\vec{\Delta d} = 3.27 \text{ m [up]}$$

$$\text{max height} = 15 \text{ m} + 3.27 \text{ m} = 18.27 \text{ m}$$

b) How fast is the egg traveling when it strikes the ground?

$$\vec{v}_i = 8.0 \text{ m/s [up]}$$

$$\vec{a}_g = 9.8 \text{ m/s}^2 \text{ (down)}$$

$$\vec{v}_f = ? \text{ Not zero!!}$$

$$\vec{\Delta d} = 15 \text{ m [down]}$$

$$\vec{v}_f^2 = \vec{v}_i^2 + 2\vec{a}\vec{\Delta d}$$

$$\vec{v}_f^2 = (8 \text{ m/s})^2 + 2(-9.8 \text{ m/s}^2)(-15 \text{ m})$$

$$\vec{v}_f^2 = 358 \text{ m}^2/\text{s}^2$$

$$\vec{v}_f = \pm \sqrt{358} \text{ m/s}$$

$$\vec{v}_f = \pm 18.9 \text{ m/s}$$

$$= -18.9 \text{ m/s}$$

$$\vec{v}_f = 18.9 \text{ m/s [down]}$$

c) How fast is the egg traveling as it passes the top of the school on the way down?

$$\vec{\Delta d} = 0$$

$$\vec{a}_g = 9.8 \text{ m/s}^2 \text{ [down]}$$

$$\vec{v}_i = 8 \text{ m/s [up]}$$

$$\vec{v}_f = ?$$

$$\vec{v}_f^2 = \vec{v}_i^2 + 2\vec{a}\vec{\Delta d}$$

$$= (8 \text{ m/s})^2 + 2(-9.8 \text{ m/s}^2)(0)$$

$$\vec{v}_f^2 = (8 \text{ m/s})^2$$

$$\vec{v}_f = \pm 8 \text{ m/s}$$

$$\vec{v}_f = 8 \text{ m/s [down]}$$

There is symmetry along the path.

d) How long is the egg in the air?

$$\vec{v}_i = 8 \text{ m/s [up]}$$

$$\vec{a}_g = 9.8 \text{ m/s}^2 \text{ [down]}$$

$$\vec{\Delta d} = 15 \text{ m [down]}$$

$$\Delta t = ?$$

$$\vec{\Delta d} = \vec{v}_i \Delta t + \frac{1}{2} \vec{a} (\Delta t)^2$$

$$-15 = 8 \Delta t + \frac{1}{2} (-9.8) \Delta t^2$$

$$-15 = 8 \Delta t - 4.9 \Delta t^2$$

$$4.9 \Delta t^2 - 8 \Delta t - 15 = 0$$

$$\Delta t = \frac{8 \pm \sqrt{(-8)^2 - 4(4.9)(-15)}}{2(4.9)}$$

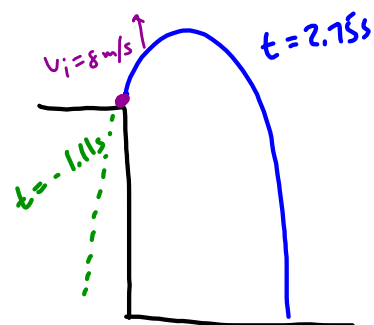
$$= \frac{8 \pm \sqrt{358}}{9.8}$$

$$\Delta t_1 = \frac{8 + \sqrt{358}}{9.8}$$

$$= 2.75 \text{ s } \checkmark$$

$$\Delta t_2 = \frac{8 - \sqrt{358}}{9.8}$$

$$= -1.11 \text{ s } \times$$



Some helpful guidelines:

When an object is dropped...

$$v_i = 0$$

$$v_f \neq 0 \quad v_f = \max v$$

When an object is launched upwards and lands at the same height...

$$\Delta d = 0$$

When an object reaches it's maximum height...

$$v = 0$$