

$$c) \frac{1 + \tan^2 x}{\cot^2 x + 1} = \tan^2 x$$

$$LS = \frac{\sec^2 x}{\csc^2 x}$$

$$= \frac{1}{\cos^2 x} \cdot \frac{1}{\frac{1}{\sin^2 x}}$$

$$= \frac{\sin^2 x}{\cos^2 x}$$

$$= \tan^2 x = RS$$

$$\text{OR } LS = \frac{1 + \tan^2 x}{\frac{1}{\tan^2 x} + 1}$$

$$= \frac{1 + \tan^2 x}{\frac{1}{\tan^2 x} + \frac{\tan^2 x}{\tan^2 x}}$$

$$= \frac{1 + \tan^2 x}{\frac{1 + \tan^2 x}{\tan^2 x}} \neq \frac{1 + \tan^2 x}{1 + \tan^2 x}$$

$$= 1 + \tan^2 x \cdot \frac{\tan^2 x}{1 + \tan^2 x}$$

$$= \tan^2 x = RS$$

$$\frac{\frac{a}{b}}{\frac{c}{d}} = \frac{a}{b} \cdot \frac{d}{c}$$

$$d) \frac{\cos^2 x \tan x}{\cot x} - 1 = -\cos^2 x$$

$$\begin{aligned} \text{LS} &= \frac{\cos^2 x \cdot \frac{\sin x}{\cos x}}{\frac{\cos x}{\sin x}} - 1 \\ &= \frac{\cos x \sin x}{\frac{\cos x}{\sin x}} - 1 \\ &= \sin^2 x - 1 \\ &= -(1 - \sin^2 x) \\ &= -\cos^2 x \\ &= \text{RS} \end{aligned}$$

P. 132  
#11, 14

$$\begin{aligned} &= \cos^2 x \left( \frac{\tan x}{\cot x} \right) - 1 \\ &= \cos^2 x \tan^2 x - 1 \\ &= \cos^2 x \cdot \frac{\sin^2 x}{\cos^2 x} - 1 \\ &= \sin^2 x - 1 \\ &= -\cos^2 x \end{aligned}$$

p.132

$$11. c) \frac{\cot x - \tan x}{\cot x + \tan x} = 2\cos^2 x - 1$$

$$LS = \frac{\frac{1}{\tan x} - \tan x}{\frac{1}{\tan x} + \tan x}$$

$$= \frac{\frac{1 - \tan^2 x}{\tan x}}{\frac{1 + \tan^2 x}{\tan x}} = \frac{1 - \tan^2 x}{\cancel{\tan x}} \cdot \frac{\cancel{\tan x}}{1 + \tan^2 x}$$

$$= \frac{1 - \tan^2 x}{1 + \tan^2 x}$$

$$= \frac{1 - \tan^2 x}{\sec^2 x}$$

$$= \cos^2 x (1 - \tan^2 x)$$

$$= \cos^2 x \left( 1 - \frac{\sin^2 x}{\cos^2 x} \right)$$

$$= \cos^2 x - \sin^2 x$$

$$= \cos^2 x - (1 - \cos^2 x)$$

$$= \cos^2 x - 1 + \cos^2 x$$

$$= 2\cos^2 x - 1 = RS$$

$$11. h) \tan^2 x + \cos^2 x - 1 = \sin^2 x \tan^2 x$$

$$LS = \tan^2 x - (1 - \cos^2 x)$$

$$= \tan^2 x - \sin^2 x$$

$$= \frac{\sin^2 x}{\cos^2 x} - \sin^2 x$$

$$= \sin^2 x \left( \frac{1}{\cos^2 x} - 1 \right)$$

$$= \sin^2 x (\sec^2 x - 1)$$

$$= \sin^2 x \tan^2 x$$

$$= RS$$