

Optimal Solutions

Goal:

- to find the optimal solution to a problem
- to correctly identify which vertices represent optimal solutions

Jane is selling apparel. She sells hats and shirts. Shirts sell for \$20 and hats sell for \$25.

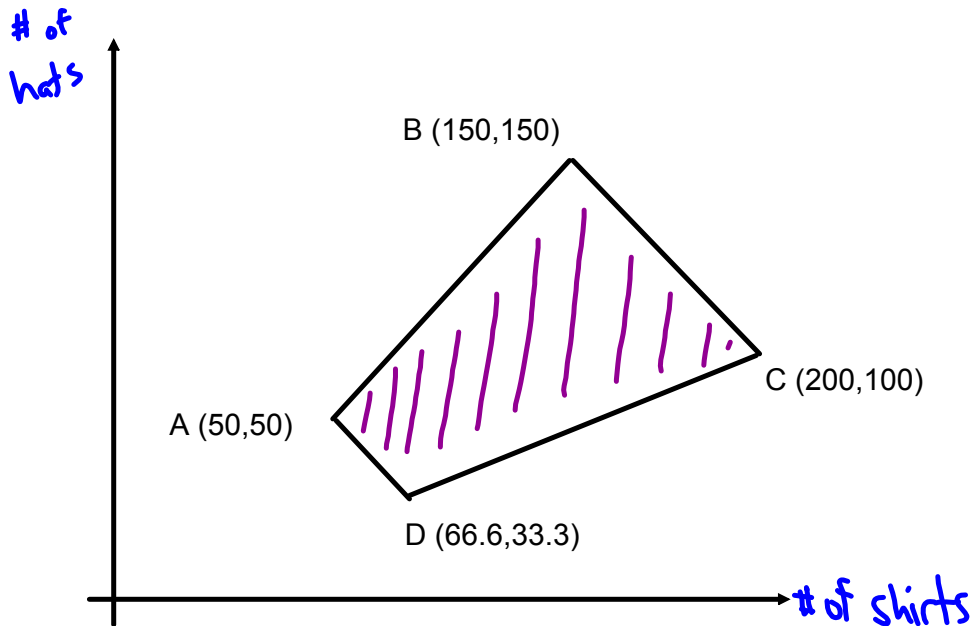
How many hats and shirts does Jane want to sell?

As many as she can!

Objective is to maximize revenues.

$$R = 20x + 25y \quad \Leftarrow \text{Target rule} \\ \text{(objective rule)}$$

Below is the polygon of constraints for Jane's situation:



How many shirts and hats does Jane want to sell?

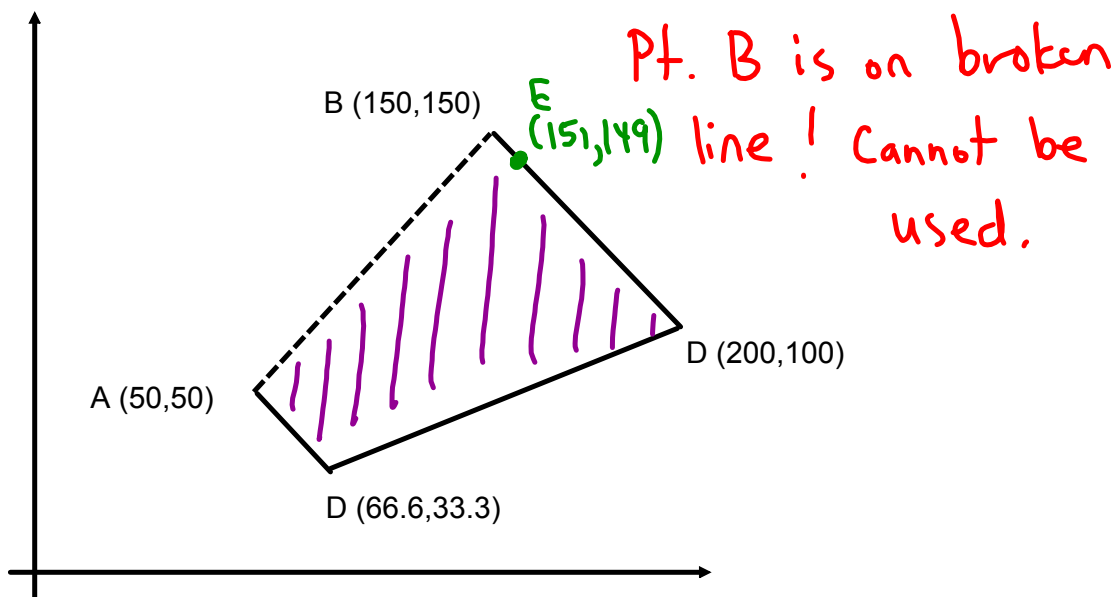
$$R = 20x + 25y$$

$$\text{Pt. B : } R = 20(150) + 25(150) = \$6750 \leftarrow \text{Max.}$$

$$\text{Pt. C : } R = 20(200) + 25(100) = \$6500$$

She should try to sell 150 shirts and 150 hats for a revenue of \$6750.

What if the polygon of constraints looked like this:



How many shirts and hats does Jane want to sell?

Since pt. B cannot be used test points near B but on polygon of constraints:

$$E(151, 149)$$

$$R = 20(151) + 25(149) = \$6745$$

To find the optimal solution:

- find the rule that describes the objective/goal
- test each vertex on the polygon of constraints to find the min or max
- remember that vertices on broken lines cannot be used